[CONTRIBUTION OF DEPARTMENT OF CHEMISTRY OF CLARK UNIVERSITY]

## Thermodynamic Quantities Associated with the Interaction between Ethylenediaminetetraacetate and Alkaline Earth Ions

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Thermodynamic equilibrium constants are reported for reactions between  $M^{+2}(aq)$  and  $V^{-4}(aq)$ , where  $M^{+2}$  is an alkaline earth ion, and  $V^{-4}$  is the tetranegative anion of ethylenediaminetetraacetic acid. The calculations were carried out with e.m.f. data obtained from cells of the type Pt-H<sub>2</sub>,  $K^{+}(m_1)$ ,  $M^{+2}(m_2)$ ,  $Cl^{-}(m_3)$ ,  $H_n V^{n-4}(m_4)$ , AgCl-Ag at various temperatures and ionic strengths. For each temperature the data were extrapolated to infinite dilution with the aid of the Debyc-Hückel activity coefficient relationship, and the thermodynamic chelate formation constant was evaluated. The thermodynamic quantities  $\Delta F^0$ ,  $\Delta H^0$  and  $\Delta S^0$  are calculated and discussed in the light of present theories of metal chelate formation in aqueous solution.

The reasons for abnormally high affinity of ethylenediaminetetraacetate and iminotriacetate anions for the alkaline earth ions have never been clarified in the light of the strongly-basic properties of these metal ions. Indeed, before the discovery of these complexing agents, the alkali and alkaline earth ions were considered to be examples of cations which did not form coördination compounds. Perhaps the most reasonable suggestion advanced to explain the high stability of chelates of this type is that of Calvin and Bailes.<sup>1</sup>

According to this theory, the entropy increase associated with the formation of chelate rings is considered to make a major contribution to the stability as measured by the equilibrium formation constant. This idea was more recently carried a step further and extended to the calcium ethylenediaminetetraacetate chelate.<sup>2</sup>

The purpose of this investigation is the determination of the experimental values of  $\Delta F^{\circ}$ ,  $\Delta H^{\circ}$  and  $\Delta S^{\circ}$  associated with chelate formation between the ethylenediaminetetraacetate ion and magnesium, calcium, strontium and barium ions. Information of this nature would be helpful in correlating the entropy effect with the formation of metal chelates of abnormally high stability.

With few exceptions, previous work on the stability of metal chelates has not resulted in the determination of thermodynamic constants, since most investigations were made in a supporting electrolyte having a concentration much higher than that of the chelate compound. The only thermodynamic chelate stability constants known to the authors of the present paper are that of Kety3 for lead<sup>II</sup> and citrate ions, of Calvin and Zebroski<sup>4</sup> for thenoyltrifluoroacetone and thorium<sup>IV</sup> ions, and of Carini and Martell<sup>5</sup> for ethylenediaminetetraacetate and calcium ions. In the present paper the latter work is extended to other alkaline earth ions, and to measurements over a series of temperatures for the calculation of heats and entropies of chelate formation.

#### Experimental

The experimental method employed in this research has not been applied previously to the determination of metal chelate stability constants. In principle, it consists of the

(1) M. Calvin and R. Bailes, THIS JOURNAL, 68, 949 (1946).

- (3) S. Kety, J. Biol. Chem., 142, 181 (1942).
  (4) E. L. Zebroski, Thesis, University of California, 1947.
- (5) F. Carini and A. E. Martell, THIS JOURNAL, 74, 5745 (1952).

measurement of hydrogen ion activities in solutions containing an alkaline earth metal ion, ethylenediaminetetraacetic acid, and inert electrolyte, at equilibrium. This was accomplished by measurement of the e.m.f. of the cell

Pt-H<sub>2</sub>, K<sup>+</sup>(
$$m_1$$
), M<sup>+2</sup>( $m_2$ ), Cl<sup>-</sup>( $m_3$ ), H<sub>n</sub>V<sup>n-4</sup>( $m_4$ ), AgCl-Ag

where  $M^{+2}$  represents an alkaline carth metal ion,  $V^{-4}$  is the ethylenediaminetetraacetate anion, and n may be varied from 0 to 2. The e.m.f. data thus obtained were extrapolated to infinite dilution, allowing the calculation of the standard free energy change,  $\Delta F^{\circ}$ , for the reaction

$$M^{+2}(aq) + V^{-4}(aq) \longrightarrow MV^{-2}(aq)$$

Apparatus and Materials.—A Leeds and Northrup type K potentiometer was used with a cell similar to that described in a previous publication.<sup>5</sup> The platinum electrodes were prepared according to the directions given by Weissberger.<sup>6</sup> The silver–silver chloride electrodes were prepared by the method of Shedlovsky and MacInnes.<sup>7</sup>

The ethylenediaminetetraacetic acid, obtained through the courtesy of the Bersworth Chemical Company, Framingham, Massachusetts, was further purified by two successive recrystallizations from water. Carbon dioxidefree potassium hydroxide, prepared from silver oxide and potassium chloride by the method of Schwarzenbach and Biedermann,<sup>8</sup> was standardized against potassium acid phthalate as recommended by Kolthoff and Sandell.<sup>9</sup> The alkaline earth chloride solutions were standardized by the Volhard method.<sup>10</sup> All solutions made up in the course of this investigation were either prepared on or corrected to a molal basis.

**Procedure and Experimental Data.**—The e.m.f. of cell I was first measured for definite values of  $m_1$ ,  $m_2$ ,  $m_1$  and  $m_4$  at 25°. The cell was then cooled to approximately 0° and the initial reading was taken. The temperature was then raised by 5° increments, and e.m.f. readings were taken after equilibrium was established. In most cases, 5–10 hours was sufficient to obtain reproducible readings, which were then found to remain constant for as long as 3 or 4 days. At 25° a check was made for reproducibility of the initial reading. The solutions employed in cell I were made up so as to give a constant ratio of  $(m_{M+1})(m_{H_N}v^{-1}):m_{MV}v^{-1}$ :  $m_{C\Gamma}$ , as is required for the extrapolation method described below (equation 13). In the more dilute solutions there was a tendency for this ratio to be changed by greater dissociation of the metal chelate. Under these conditions the ratios were maintained by appropriate addition of potassium hydroxide. These ratios were kept constant for each

(6) A. Weissberger, "Physical Methods of Organic Chemistry," Second Edition, Vol. II, Interscience Publishers, Inc., New York, N. Y., 1949, p. 1722.

(7) T. Shedlovsky and D. A. MacInnes, This Journal, **58**, 1970 (1936).

(8) G. Schwarzenbach and W. Biedermann, Helv. Chim. Acta, 31, 331 (1948).

(9) I. M. Kolthoff and E. B. Sandell, "Textbook of Quantitative Inorganic Analysis," Revised Edition, The Macmillan Co., New York. N. Y., 1948, p. 553.

(10) W. Scott, "Standard Methods of Chemical Analysis," Fifth Edition, Vol. I, D. Van Nostrand Co., Inc., New York, N. Y., 1939, p. 271.

			,	Table I			
1.00	Metal	a		E.m.f. (my	.) of cell I		a
, C. 0	Ma	н. 653 19	μ2" 642-15	#3~ 620 16	μ4* 694 10	#6* 620 02	μ6~
0	Ca	539 91	530 32	594 69	521 81	518 45	515 26
	Sr	628.95	624 02	616 00	613 56	610 74	606.08
	Ba	620.00 621.25	610 69	606 84	602.77	600.01	000.08
5	Σu Ma	657.20	647 12	649.17	627.07	400.01 400 SD	
		542 06	532 20	526 50	592 41	000.80 590.96	517 99
	Sr	635 49	630 41	622 30	610 76	616 05	612 15
	Ba	624 78	614 19	610 21	606 02	603 37	012,10
to	Ma	661 67	651 99	646 16	611 90	607.60	
10	Ca	544 65	534 65	528 60	595 77	599 51	510.96
	Sr	640 77	625 55	627.90	624.52	691 94	617 20
	Ba	628 41	617 74	613 58	609.31	606.56	017.20
15	 Mo	665 67	654 97	640.80	615 54	641.90	
10	Ca	546 92	536 86	520 74	597 89	594 51	591 95
	Sr	645 66	640 45	632 16	620 42	626 27	621.20
	Ba	631.93	621.19	616 73	612,50	609.75	021.00
20	Ma	660 11	658 30	652.00	618 64	644 99	
20	Ca	540 30	538 05	529.78	520 76	526 62	592 01
	Sr	650 74	645 27	636 83	633 03	630.00	626 07
	Ba	635 67	624 39	620.20	615 90	613 22	020.07
05	Ma	673.06	662.00	656 69	650 19	647.75	
20	Co	551 26	540.70	524 46	521 45	047.70 597 06	594 64
	Ca Sr	654 43	640 34	640 77	628 16	624 70	620.06
	Ba	639 05	627 63	623 26	619 00	615 99	050.00
20	Ma	677.20	665 92	660.26	655 05	651 00	
30		553 30	542 65	526 21	000,80 529,07	001.28 590.78	596 17
	Sr	658.37	652.96	644 18	642 01	638 46	633 65
	Ba	$642 \ 37$	630.77	626 19	621 92	618 80	000.00
	2500			Molal concent	ration $\times 10^3$	010.00	
Motel	Ma	8 594	$\frac{1}{1000} = \frac{1100}{1100} = \frac{15}{100} = $				
Aoid	Mg	0.354	1 2521	14.001	2 0626	21.00 9.5129	
	0	10.0072	01 640	1.700+	2.0020	2.0102	10.00
Metal	Ca	1.3,810	21.043	28.66	32,89	38.14	43.90
Acia	0	2,1957	0.249	4.214	+.481	5.096	5.711
Metal	Sr	7.283	9.153	13.246	14.978	17.021	20.39
Acid	_	1,1451	1,8306	2.061	2,320	2.629	3,141
Metal	Ва	13.342	22.32	27.29	33.02	37.49	
Acid		2.005	3.355	4.102	4.963	5.649	

<sup>a</sup> The values of  $\mu_1$ ,  $\mu_2$ ,  $\mu_3$ , etc., differ for each e.m.f. measurement, and may be found as points in Fig. 1.

Sample e.m.f. data for cell I obtained at 0, 5, 10, 15, 20, 25 and  $30^{\circ}$  for each of the four alkaline earth ions at various ionic strengths are given in Table I. Because of space limitations only one value is given for each set of conditions, and all duplications and minor variations are omitted.

**Calculations.**—The e.m.f. of cell I is given by the equation

$$E = E^{\circ} - RT \ln a_{\mathrm{H}^{+}} m_{\mathrm{Cl}^{-}} \gamma_{\mathrm{Cl}^{-}}$$
(1)

where  $\gamma$  represents activity coefficient and the other terms have their usual meaning. The stability of the metal chelate is defined in terms of the chemical equilibrium

$$M^{+2} + V^{-4} \xrightarrow{\longrightarrow} MV^{-2}$$

where  $M^{+2}$  represents an alkaline earth ion and  $V^{-4}$  represents the tetravalent anion of ethylenediaminetetraacetic acid. The corresponding stability constant expression is

$$K = \frac{a_{\rm M} v^{-2}}{a_{\rm M}^{+2} \times a_{\rm V}^{-4}} \tag{2}$$

At the pH employed in the experimental solutions for cell I, it is necessary to take into account the

$$H_2 V^{-2} \xrightarrow{\longrightarrow} H^+ + H V^{-3}$$
$$H V^{-3} \xrightarrow{\longrightarrow} H^+ + V^{-4}$$

The corresponding thermodynamic acid dissociation constants are defined by

$$k_3 = \frac{a_{\rm H^+} \times a_{\rm HV^{-3}}}{a_{\rm H_2V^{-2}}} \tag{3}$$

$$k_4 = \frac{a_{\rm H^+} \times a_{\rm V^{-4}}}{a_{\rm HV^{-3}}} \tag{4}$$

Rearrangement of equations (2), (3), and (4) gives

$$a_{\rm H^+} = \left(\frac{a_{\rm M^{+2}} \times a_{\rm H_2V^{-2}}}{a_{\rm MV^{-2}}} k_3 k_4 K\right)^{1/2} \tag{5}$$

Combination of equations 1 and 5 results in the relationship

$$\frac{(E - E^0)F}{2.3RT} + \log m_{\rm Cl^-} = -\frac{1}{2}\log \left(\frac{a_{\rm M}^{*2} \times a_{\rm H2}v^{-2}}{a_{\rm M}v^{-2}}k_3k_4K\right) - \log \gamma_{\rm Cl^-} \quad (6)$$

Rearrangement of 6 with the substitution of  $m_s \gamma_s$ for  $a_s$  and of  $p_w H$  for  $(E - E^\circ) F/2.3 RT + \log$  $m_{\rm Cl}$ -, according to standard practice, results in the relationship

$$p_{\rm w}H - \frac{1}{2}(pk_3 + pk_4) + \frac{1}{2}\log\frac{m_{\rm M}^{+2} \times m_{\rm H_2}v^{-2}}{m_{\rm M}v^{-2}} = -\frac{1}{2}\log K - \frac{1}{2}\log\frac{\gamma_{\rm M}^{+2} \times \gamma_{\rm H_2}v^{-2} \times \gamma^2_{\rm Cl^-}}{\gamma_{\rm M}v^{-2}}$$
(7)

The activity coefficient term was defined as a function of ionics trength in terms of an arbitrary parameter,  $a^*$ , the "distance of closest approach" obtained from the Debye-Hückel relationship

$$-\log \gamma_{i} = \frac{A Z_{i}^{2} \sqrt{\mu}}{1 + B a_{i}^{*} \sqrt{\mu}} + \beta m_{i}$$
(8)

where A, Z and B have their usual significance. The quantity  $\beta$  was evaluated by the method described by Hamer and Acree.<sup>11</sup> Since the properties of each ionic species present in the mixture are additive functions of those of the individual ions present, it follows that  $\Sigma \beta m_i = \Sigma (1/n) \beta_i n \mu_i$ . If the ionic strength contribution of each ion is some fraction of the total ionic strength (*i.e.*,  $\mu_i$  = constant  $\times \mu$  where p, q and r are constants for a specified ratio of salts) and since  $\mu_i = nm_i$  and  $\mu =$  $\Sigma \mu_i$ , it follows that

$$\frac{1}{n_{\rm i}} (p\beta_{\rm i}n)\mu - \frac{1}{n_{\rm i}} (q\beta_{\rm i}n)\mu - \frac{1}{n_{\rm k}} (r\beta_{\rm k}n)\mu = \beta\mu \quad (9)$$

The relationship derived from equation 8 to fit the requirements for the extrapolation of the quantities of equation 7 to infinite dilution is

$$-{}^{1}/_{2}\log\frac{\gamma_{\rm M^{+2}} \times \gamma_{\rm H_{2}V^{-2}} \times \gamma^{2}_{\rm CI^{-}}}{\gamma_{\rm MV^{-2}}} = \frac{3A\sqrt{\mu}}{1 + Ba^{*}\sqrt{\mu}} + \beta\mu \quad (10)$$

The values of  $\beta$  obtained by means of equation 9 and the values arbitrarily selected for the constant  $a^*$  so as to give a straight-line extrapolation of equation 7 with minimum slope were substituted into equation 10 to give values of log  $\gamma_r$ , equal to the quantity  $-1/_2 \log (\gamma_{M^{+2}} \times \gamma_{H_2V^{-2}} \times \gamma^2_{Cl} / \gamma_{MV^{-2}})$  for each temperature and each metal ion system. The values of log  $m_{M^{+2}}$   $(m_{H_2V^{-2}}/m_{MV^{-2}})$  were calculated and listed in Table II as  $\log r$ , along with the values of  $a^*$  and  $\beta$ , determined as described above.

All the terms in the resulting relationship for equation 7 with the exception of K were placed on the left side of the equation and extrapolated as a function of ionic strength to infinite dilution. Thus, the thermodynamic constant K was evaluated for each temperature investigated. The graphical extrapolations to infinite dilution are given in Fig. 1. The values of  $pk_3$  and  $pk_4$  used in equation 7 were reported in an earlier publication.12

The standard thermodynamic quantities  $\Delta F^{\circ}$ ,  $\Delta H^{\circ}$  and  $\Delta S^{\circ}$  were calculated by means Fig. 1.—Extrapolation of potentiometric data to infinite dilution of the usual relationships

$$\Delta F^{0} = -2.303 RT \log K$$
(11)  
$$\Delta H^{0} = \frac{2.303 RT_{1}T_{2} (\log k_{2} - \log k_{1})}{T_{2} - T_{1}}$$
(12)

(11) W. Hamer and S. Acree, J. Research Natl. Bur. Standards, 35, 381 (1945).

(12) F. F. Carini and A. E. Martell, This Journal, 75, 4810 (1953).

$$\Delta S^0 = \frac{\Delta H^0 - \Delta F^0}{T} \tag{13}$$

ACTIVITY	COEFFICIENT	S
$a^*$	β	$\log r$
6.0	0.7	2.759
6.0	.7	2.804
6.0	.6	2.856
	a* 6.0 6.0 6.0 6.0	ACTIVITYCOEFFICIENT $a^*$ $\beta$ $6.0$ $0.7$ $6.0$ $.7$ $6.0$ $.6$

TADT T II

	15	6.1	.6	2.914
	20	6.1	.5	2.953
	25	6.2	.5	3,008
	30	6.2	.5	3.026
$Ca^{+2}$	0	10.3	1.0	1.025
	5	10.4	1.0	1.087
	10	10.4	0.9	1.156
	15	10.5	.9	1.235
	20	10.6	.9	1.309
	25	10.7	.9	1.380
	30	10.8	.9	1.446
Sr +2	0	10.5	0.8	1.716
	5	10.6	.8	1,840
	10	10.7	.7	1.932
	15	10.8	.7	2.023
	20	10.9	.7	2.116
	25	11.0	.6	2.189
	30	11.0	.5	2.248
Ba +2	0	6.0	0.6	0.811
	5	6.1	.6	.840
	10	6.2	.6	.879
	15	6.4	.6	.934
	20	6.5	.6	.983
	25	6.6	.6	1.029
	30	6.7	.6	1.069



(see equation 7).

The equilibrium constants and thermodynamic constants calculated by means of equations 7, 11, 12 and 13 are given in Table III.

## Discussion

From the equilibrium formation constants listed

TABLE III						
°C.	Mg	Ca	Sr	Ва		
		log K				
()	9.28	11.14	9.02	8.01		
5	9.24	11.12	8,96	7.95		
10	9.20	11.08	8.91	7.89		
15	9.16	11.04	8.85	7.84		
<b>20</b>	9.12	11.00	8.80	7.78		
25	9,09	10.98	8.76	7.73		
30	9.05	10.95	8.74	7.68		
		$-\Delta F^0$ , kcal				
0	11.60	13.92	11.33	10.01		
$\overline{5}$	11.77	14.15	11.44	10.12		
10	11.92	14.35	11.54	10.22		
15	12.08	14.55	11.66	10.33		
20	12.24	14.76	11.80	10.44		
25	12.40	14.97	11,90	10.54		
30	12.56	15.18	12.11	10.66		
$- \Delta H^0$ , kcal.						
0-30	2.9	2.5	4.1	4.1		
$+ \Delta S^0$ , e.u.						
0-30	32	42	26	22		

in Table III, it is seen that the order of stability of the 1:1 alkaline earth chelates of ethylenediaminetetraacetic acid is: Mg(II) > Ca(II) > Sr(II) > Ba(II). This is the same order as was found by Schwarzenbach and Ackermann<sup>13</sup> on the basis of "concentration" constants in 0.1 *M* KCI at 20°, although the thermodynamic values of the present investigation are considerably higher, as expected. Although the stability as measured by the equilibrium constants decreases slightly with an increase in temperature, the values of  $-\Delta F^{\circ}$  increase in magnitude as the temperature increases.

The enthalpies of formation of the metal chelates from the aqueous ions in their standard states are seen from the values of  $\Delta II^{\circ}$  in Table III to be all small, negative, and about the same magnitude. These values correspond to the breaking of the M–H<sub>2</sub>O bonds of the hydrated ions and the formation of the metal-ligand bands in the chelates. Thus, if one neglects the slight amount of hydration of the ligand anion, the reactions involved in the calculated  $\Delta II^{\circ}$  values may be summarized by the equation



The heats of hydration of the alkaline earth metal ions are 448, 362, 334 and 288 kcal./mole for Mg-(II), Ca(II), Sr(II) and Ba(II), respectively.<sup>14</sup>

(13) G. Schwarzenbach and H. Ackermann, Helv. Chim. Acta, **30**, 1798 (1947).

(14) A. Smekal, "Handbuch der Physik," 12th Ed., Vol. 24, part II, Julius Springer, Berlin, 1933, p. 1051. Since the value of  $\Delta II^{\circ}$  determined in this investigation is quite small compared to heats of hydration, it seems that the heats of formation of the metal chelate bonds are of approximately the same magnitude as the ion-dipole bonds of the hydrated ions.

The most significant result of this investigation is the fact that the high stability of the alkaline earth-ethylenediaminetetraacetate chelates is due primarily to the large entropy increase associated with complex formation. The entropy change accounts for from about two-thirds of the free energy increase for the barium chelate to about fourfifths for the calcium chelate. An entropy increase would be expected for a system such as this where the charge of the ions is decreased, where the ion formed is larger than the ions from which it is produced (to allow a more favorable distribution of charge), and where an increase in the number of particles occurs. From the equation given above it is readily seen that all three factors operate in this case. The latter effect, in which the highly polarized water molecules surrounding the metal ions are released to the body of the solution, is believed to be the most important of the three. The original suggestion of Calvin and Bailes<sup>1</sup> for the copper(II)-salicylaldehyde chelate attributed the greater part of the stability to the same type of entropy effect.

The fact that the reported entropy changes increase to a maximum with the calcium ion and then decrease again for the larger ions is interesting as a comparison of relative tendencies for chelate ring formation. It is probable that the coördination number of the magnesium ion is somewhat less than that of the other ions of the alkaline earth group. The release of fewer water molecules to the solvent in the case of the magnesium ion seems to correlate with the fact that the observed entropy change is less favorable than that of the calcium ion. The smaller magnitudes of the entropy increase for strontium and barium may be due to the introduction of strain in the chelate rings involving the larger ions.

The reasons for the high affinity of the ethylenediaminetetraacetate anion for alkaline earth ions has been a matter of speculation for some time. One of the chief difficulties is the fact that the highly basic alkaline earth ions are generally recognized as having little affinity for all complexing agents and most chelating agents. The formation of multiple chelate rings and the consequent entropy effect is in itself unsatisfactory, since other polydentate ligands, such as the polyamines, would otherwise form strong chelates with the alkaline earth ions. Therefore, it seems that a negative or very small positive value of  $\Delta H^{\circ}$  is also an essential requirement for a stable chelate. The formation of alkaline earth chelates of the polydentate polyamines would probably involve a favorable entropy increase but a highly unfavorable (*i.e.*, relatively large and positive) enthalpy (i.e., relatively)change. Thus, the fact that the affinity of the donor groups in the ethylenediaminetetraacetate anion for calcium ion is at least as great as that of water molecules is fundamental to the attainment of high stability in the resulting chelate. Acknowledgment.—The authors are indebted to the U. S. Navy Office of Naval Research for support of this research project under Contract Nonr-596(00).

WORCESTER, MASS.

[CONTRIBUTION FROM THE CHEMISTRY DEPARTMENT, UNIVERSITY OF TORONTO]

# The Determination of the Adjusted Indicator Concentration behind a Moving Boundary in Dilute Solution; the System Potassium Chloride–Sodium Chloride in Water at 25°

BY D. R. MUIR, J. R. GRAHAM AND A. R. GORDON

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A method is described for determining the adjusted indicator concentration behind a moving boundary in dilute solutions. To test the procedure, the system KCl-NaCl was investigated. It is shown that the Kohlrausch ratio can be determined with a precision comparable with that obtainable in moving boundary determinations of transference numbers, and that the ratio, measured over a range of concentration, can be extrapolated unambiguously to zero concentration. From the limiting ratio and the limiting equivalent conductances of leading and indicator salts, limiting ionic conductances may be obtained at once. Thus limiting ionic conductances can be determined in any solvent in which precise conductance measurements are possible, without carrying out any transference measurements in the ordinary sense of the term. Possible applications of the method are discussed.

In 1934, Hartley, Drew and Collie<sup>1</sup> reported a method for measuring the transference number of a slow ion by determining the adjusted indicator concentration of that ion behind a boundary for which the transference number of the leading fast ion was known. The basis for the procedure was the familiar Kohlrausch<sup>2</sup> condition for a stable two salt boundary of the type  $MA/M_iA$ 

$$C_{\rm i}/C = t_{\rm i}/t = r \tag{1}$$

where C and  $C_i$  are the concentrations of the leading and indicator ions M and  $M_i$ , respectively, t and  $t_i$  are the corresponding transference numbers, and r is the Kohlrausch ratio. As originally developed, the method was not capable of high precision, but it did permit approximate determinations of the transference numbers of certain paraffin-chain salts.3 Years later, and using modern techniques, analogous measurements were carried out by Longsworth<sup>4</sup> to test the Dole theory<sup>5</sup> of polysalt boundaries, but on the whole the possibility of obtaining reasonably precise transference data in this way has received little attention. In a recent paper<sup>6</sup> dealing with adjustment of indicator concentration during moving boundary measure-ments, it was shown that with the type of cell there employed, it was possible to determine the indicator concentration behind the boundary within a part in 500 or so; this suggested that if the precision of such measurements could be raised to a level comparable with that obtainable in the usual moving boundary determination, and that if the Kohlrausch ratio, measured over a range of concentrations, could be extrapolated to infinite dilution, the resulting limiting ratio could be combined with the corresponding limiting equivalent conductances to yield limiting ionic conductances. Since limiting ionic conductances provide information as to ion-

(1) G. S. Hartley, E. Drew and B. Collie, Trans. Faraday Soc., 30, 648 (1934).

(2) F. Kohlrausch, Ann. Physik. Chem., 62, 209 (1897).

(3) G. S. Hartley, B. Collie and C. S. Samis, *Trans. Faraday Soc.*, 32, 795 (1936).

(4) L. G. Longsworth, THIS JOURNAL, 67, 1109 (1945).

(5) V. P. Dole, ibid., 67, 1119 (1945).

(6) A. R. Gordon and R. L. Kay, J. Chem. Phys., 21, 131 (1953).

dipole interaction unobtainable from the equivalent conductance data, and since the procedure outlined above would eliminate the need for transference measurements in the ordinary sense of the term, it seemed desirable to investigate this possibility.

The system chosen for investigation was KCl/ NaCl in aqueous solution at  $25^{\circ}$ . The reasons for this choice were first, that for both salts the transference numbers were well established,<sup>7-9</sup> and second, that owing to the relatively rapid change of the transference number for NaCl with concentration as compared with that for KCl, this system provided a good test of any extrapolation procedure.

#### Experimental

A series of tests with the cells previously employed (see Fig. 2 of ref. 6) and with various modifications of them, showed that the desired precision in the measurement of the adjusted indicator concentration (0.02%) could not be attained, but partly by accident it was found that a much simpler technique could, with care, provide data of the accuracy desired. Essentially the cell is a conventional falling boundary cell of the type used for many years in this Laboratory with a type VIII shearing mechanism (see Fig. 1 of ref. 6). It differs only in that the channel is somewhat longer (approximately 30 cm.) than in earlier cells, and that there is an additional shearing stopcock at the base of the channel. As in earlier cells, the channel is 2.5 mm. internal diameter and cadmium and silver-silver chloride electrodes serve as anode and cathode. To fill, KCl solution is forced upward into the channel until it rises just above the top of the upper shearing stopcock, which is then closed. The reservoir above the stopcock is then repeatedly flushed with the NaCl solution; after filling, the cell is brought to tem-perature equilibrium in a bath regulated to  $\pm 0.01^\circ$ , the junction is formed at the top of the channel, and the current is started. It should be noted that only an approximate knowledge of the current and the time of electrolysis is necessary. Fifteen or twenty minutes after the time calculated for the boundary to pass the lower stopcock, the current is stopped and both cocks closed, thus isolating a column of indicator solution. For a system for which the transference number of the leading ion was not known, a preliminary series of measurements would obviously be required to determine the length of electrolysis necessary for the concentration of the solution in the channel to become independent of further passage of current.

<sup>(7)</sup> L. G. Longsworth, THIS JOURNAL, 54, 2741 (1932).

<sup>(8)</sup> R. W. Aligood, D. J. LeRoy and A. R. Gordon, J. Chem. Phys., 8, 418 (1940).

<sup>(9)</sup> R. W. Allgood and A. R. Gordon, ibid., 10, 124 (1942).